Exercise 1

Question B1: Oxygen Intake on a Treadmill

A group of athletes volunteered to have their oxygen intake measured whilst running on a treadmill.

The treadmill allows for adjustments to the incline of the run and to the speed at which the belt of the treadmill rotates.

The treadmill's running power can be adjusted by increasing the speed of the treadmill as well as increasing the incline of the run.

In the table, below, you will find data for the volunteer athletes' intake of oxygen, in litres per minute, for different levels of treadmill running power, in Watts.



Power (Watts)	30	60	90	120	150	180
Oxygen intake (litres/minute)	1.54	2.56	3.45	4.08	4.61	4.93

a) Draw a scatter diagram showing oxygen intake, in litres per minute, on the vertical axis, as a function of power, in Watts, on the horizontal axis.
Scale of Avec: Represent 10 Watts as 0.5 cm on the horizontal axis and one litre/minute as

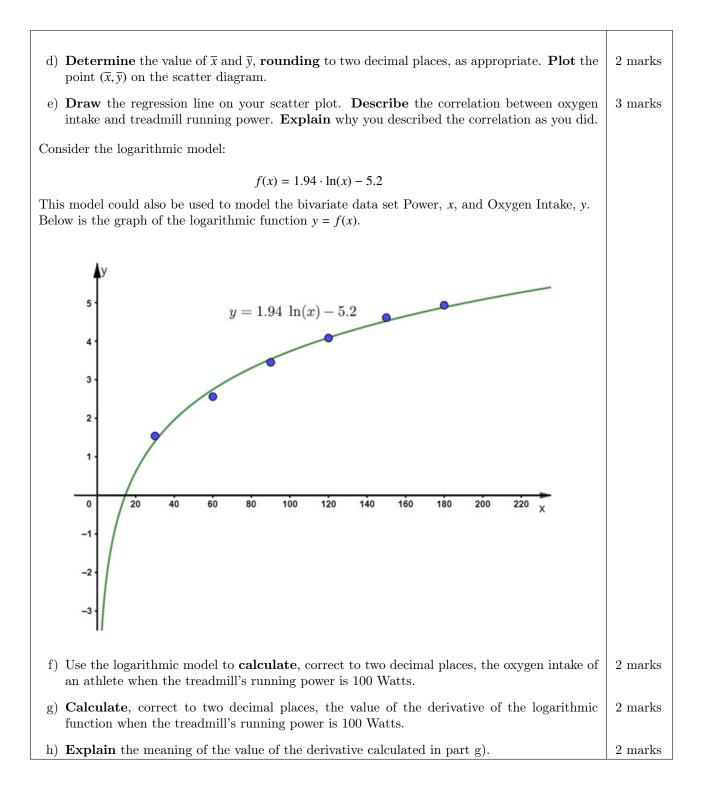
Scale of Axes: Represent 10 Watts as 0.5 cm on the horizontal axis and one litre/minute as 1 cm on the vertical axis.

The data can be modelled using a linear function $y = a \cdot x + b$ where y is the oxygen intake and x is the power.

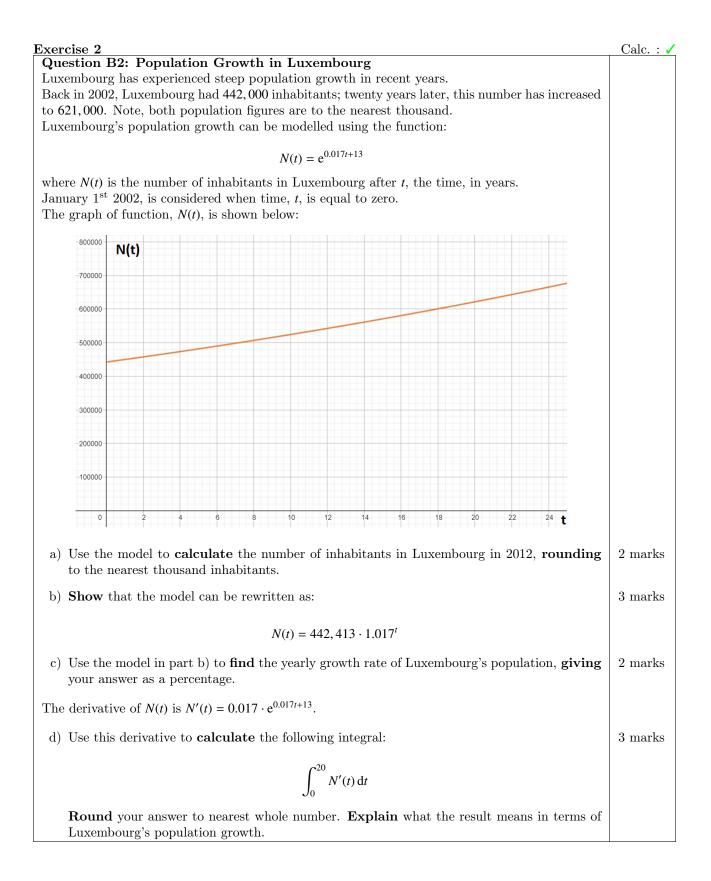
- b) Use your calculator to **find** the equation of the line of regression of *y* on *x*, **giving** the values 2 marks of *a* and *b* correct to three decimal places.
- c) Use the line of regression, from part b) to **calculate**, correct to two decimal places, the oxygen intake of an athlete running on a treadmill with a power of 200 Watts.

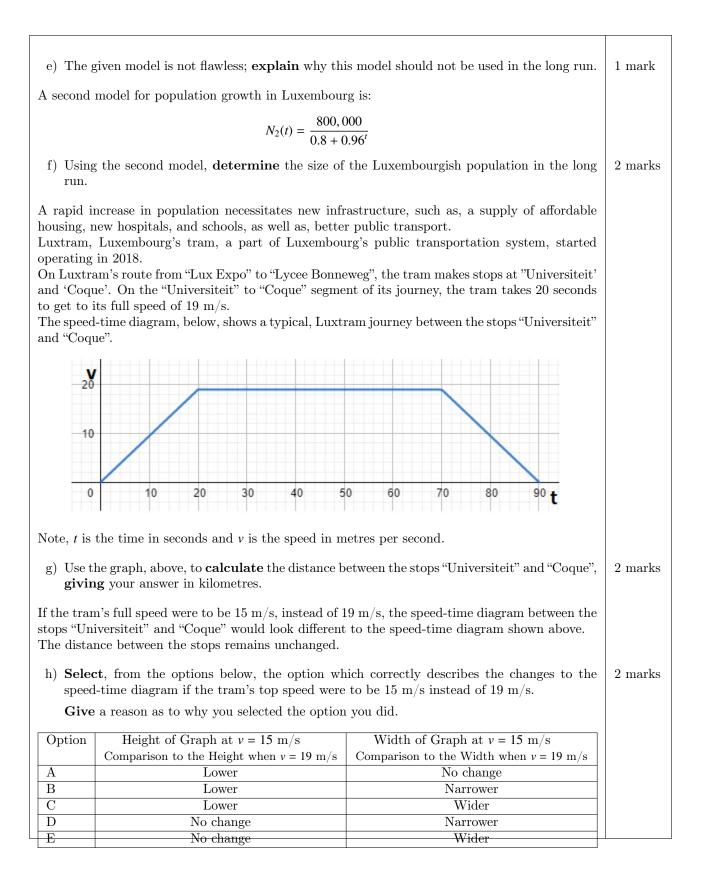
If you didn't find values for a and b in part b) please use a = 0.02 and b = 1.16.

Calc. : 🗸



An athlete would like to adjust the treadmill's running power to permit an oxygen intake of exactly 3 litres/minute.		
i) Use the logarithmic model to determine , correct one decimal place, the power level at which the treadmill must be set, to permit an oxygen intake of three litres/minute.		
Both the linear model and the logarithmic model fit well to the given data points. However, when using the models for interpolation or extrapolation, one model falls short i.e., it is not as appropriate as thought.		
j) Select the appropriate word(s) from the list:		
Word Choices		
A: Linear		
B: Logarithmic		
C: Interpolation		
D: Extrapolation		
to complete the sentence below.		
"The model should not be used for"		
$\mathbf{Write} \ the \ entire \ sentence \ on \ your \ exam \ script. \ \mathbf{Provide} \ reasoning \ for \ your \ choice \ of \ word(s).$		
In the group of volunteer athletes, 60% were football players, 30% were cross-country runners and 20% of the athletes did neither of these two sports.		
k) Given that an athlete plays football, calculate the probability that this athlete isn't a cross- country runner.		
 Out of the 12 Venn diagrams, numbered one through twelve, given below, choose the Venn diagram where the shaded region, matches the probability that you were asked to calculate in the part k). 		
1. $\begin{bmatrix} c \\ c $		
5. \mathbb{F} 6. \mathbb{F} 7. \mathbb{F} 8. \mathbb{F} 6.		
9. F C 10. F C 11. F C 12. F C		





As Luxembourg's public transport is free; the tram is a popular means of transport for many students. Luxtram knows that, on a usual school day, 1,500 passengers take the tram, 35%, of whom, are high school students. Note: Passengers travel independently of each other.	
Let X be the number of high school students who take the tram, out of the 1,500 passengers, who take the tram on a usual school day.	
i) Explain why X is binomially distributed, stating the parameters of this binomial distribution.	2 marks
j) Calculate the expected value and the standard deviation of the number of high school students taking the tram, on a usual school day, rounding to two decimal places where appropriate.	2 marks
k) Calculate , correct to three decimal places, the probability that, on a usual school day, at most 500 high school students use the tram.	2 marks
1) Determine , on a day which is not a usual school day, the total number of passengers taking the tram, if it were expected that 630 high school students would be taking the tram.	2 marks