Exercise 1	Calc. : 🗸					
The methane molecule CH_4 , represented opposite, can be modeled by a regular tetrahedron OABD, with $O(0;0;0)$, $A(3;\sqrt{3};2\sqrt{6})$, $B(3;3\sqrt{3};0)$ and $D(6;0;0)$. The four vertices are the positions of the hydrogen atoms H. We are interested in this exercise in the position of the carbon atom C, inside this tetrahedron. This position is represented by a point that we call G.						
1. The tetrahedron is regular, so all of its edges have the same length. Justify that this length is equal to 6.						
2. Justify that the coordinates of the orthogonal project A' of A on the plane (Oxy) with equation $z = 0$ are A' (3; $\sqrt{3}$; 0).						
3. The point G is the intersection of (AA') and (IJ), where $I\left(\frac{3}{2}; \frac{\sqrt{3}}{2}; \sqrt{6}\right)$ is the middle of segment						
[AO] and $J\left(\frac{9}{2};\frac{3\sqrt{3}}{2};0\right)$ the middle of the segment [BD].						
(a) Prove that the coordinates of G are $\left(3; \sqrt{3}; \frac{\sqrt{6}}{2}\right)$.						
(b) Check that the distance between G and A is equal to $\frac{3\sqrt{6}}{2}$.	1 mark					
We admit that it is also the distance between G and the other vertices of the tetrahedron.						
(c) In reality, the length of the C–H bond is approximately equal to 109 picometers. Deter- mine an approximate value, in picometers, the distance between two hydrogen atoms.						
4. Give an approximate value of the measure of the angle formed by two C–H bonds.	3 marks					

Exercise 2

xercise 2	Calc. : 🗸				
1. Let the complex number $w = \frac{1}{4} + \frac{1}{4}i$.					
(a) Write w in exponential form.					
(b) Determine the values of the natural number n for which w^n is a real number.					
2. For any natural number n , we note M_n the affix point z_n defined by:					
$\begin{cases} z_0 = 1 \\ z_{n+1} = \left(\frac{1}{4} + \frac{1}{4}\mathbf{i}\right) \cdot z_n, n \in \mathbb{N} \end{cases}$					
(a) Calculate z_1 and z_2 , then place in the complex plane the points M_0 , M_1 , M_2 (graphical unit: 4 cm).	2 marks				
(b) Let r be the sequence defined, for any natural number n, by $r_n = z_n $.	3 marks				
Show that the sequence r is geometric with commonality $\frac{\sqrt{2}}{4}$.					
Deduce an expression of r_n as a function of n .					
(c) We assume that for any natural number $n, z_n = r_n e^{\frac{in\pi}{4}}$.	$1 \mathrm{mark}$				
Under what condition does the point M_n belong to the real axis?					
(d) Describe the precise position of the point M_{10} which represents z_{10} in the complex plane.	2 marks				



Exercise 4								Calc. : 🗸
In this exercise, all results will be round	led to 3	decima	al places	. <u>.</u>				
1. Here is the evolution of sales of el 2017.	ectrical	ly assis	ted bicy	ycles in	France	betwee	en 2007 and	
Year	2007	2009	2011	2013	2015	2017]	
Rank of the year x_i	0	2	4	6	8	10	-	
Number of e-bikes sold (thousands): n_i	10	23	37	57	102	278		
Data: Observatoire du Cycle							-	
(a) Using the calculator, determine correlation coefficient.	an affii	ne adjus	stment o	of n in z	x for th	is data.	Specify the	2 marks
(b) We set $y_i = \ln(n_i)$. In this case, a affine adjustment of y in x is given by the formula $y = 0.307x + 2.353$, with a correlation coefficient approximately equal to 0.981.								2 marks
Use best-fit model to extrapolat	e bike s	sales of	this typ	be in 20	23.			
2. A company mass-produces power-assisted bicycles. Either X the random variable which, for each bike taken at random in the production associates its autonomy, in kilometres. We admit that this random variable X follows a normal law.								
We know that $P(X \geq 84) = 0.2266$ a	nd $P(X$	≤ 86) =	0.8943					
Determine the mean and the standard deviation of this law. Round the results in km to the nearest integer.								4 marks
3. In this part, it is considered that 4% as "non-compliant".	% of lith	ium-ior	n batter	ies have	a defec	et and a	re described	
Let Y be the random variable which, for any batch of 150 batteries taken randomly in production, associates the number of batteries not compliant.								
The production is large enough for u in a draw with replacement.	is to be	able to a	assimila	te such	a collec	tion of 3	150 batteries	
(a) Determine $P(Y \leq 5)$ by specifyin	ng the c	hosen n	nodel.					2 marks
(b) Determine the probability that compliant. Interpret the result.	, in a r	andom	sample	of 150	batteri	es, all l	patteries are	2 marks