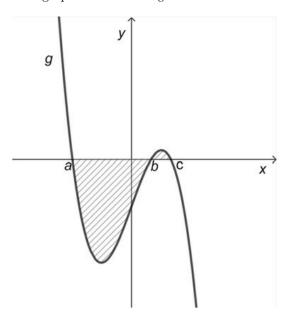
$$f(x) = 2x^3 - 9x^2 + 45.$$

Determine the coordinates of the extrema of the function f and specify their nature.

5 marks

Exercise 2 Calc.: X

The diagram below shows the graph of a function g.



Specify for each of the following expressions, whether it represents the hatched area. **Justify** 5 marks your answer.

a)
$$\int_{a}^{c} g(x) dx$$

b)
$$\int_a^b g(x) \, \mathrm{d}x + \int_b^c g(x) \, \mathrm{d}x$$

c)
$$\left| \int_{a}^{c} g(x) \, \mathrm{d}x \right|$$

d)
$$-\int_a^b g(x) dx + \int_b^c g(x) dx$$

Exercise 3 Calc.: X

A car is travelling along a horizontal road and the distance from the origin is observed over a period of 8 seconds, starting at t = 4 seconds.

The distance is given by the function d defined by

$$d(t) = \frac{1}{4}t^3 - 2t^2 + 5t + 3 \qquad \text{with } t \in [4, 12],$$

where t is the time expressed in seconds, and d(t) is expressed in metres.

a) Show that at the start of the observation, the car is 7 metres from the origin.

 $1 \, \text{mark}$

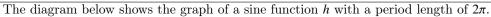
b) **Determine** the average velocity of the car between 4 seconds and 10 seconds.

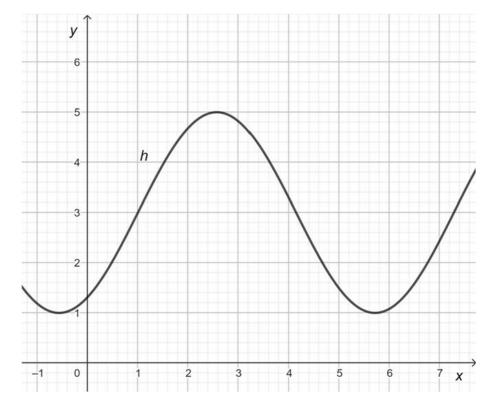
2 marks

c) **Determine** the instantaneous velocity of the car at t = 10 seconds.

2 marks

Exercise 4 Calc.: X





Determine h(x).

Exercise 5 Calc.: X

Between 1st January 2000 and 1st January 2023, a group of scientists studied the surface area of a lake in a mountainous region of Europe. They created a model which suggests that the surface area of the lake decreases by 10% each year.

The initial surface area of the lake is 5 km².

a) **Explain** why the surface area of the lake can be modelled by a function s defined by $s(t) = 5 \cdot 0.9^t$, where t is the number of years since year 2000 and s(t) is expressed in km².

b) Using this model, **determine** the surface area of the lake in 2002.

c) Assume the model will remain valid over time.

Describe the evolution of the surface area of the lake over time.

Exercise 6 Calc. : X

Peter applies for his first job. He sends his CV letter to 2 different companies. The probability that exactly one company will reply to him is 0.45.

The probability that no company will reply to him is 0.3.

a) **Draw** a Venn diagram to illustrate the above information.

2 marks

b) **Determine** the probability that both companies will reply to Peter. **Give** the answer as a percentage.

3 marks

2 marks

Exercise 7

The distribution of peppers at a grower's market stand is as follows:

\[\frac{2}{5} \] of peppers are green, of which half are organic.

\[\frac{9}{20} \] of peppers are red, of which 40\% are organic.

\[\frac{3}{20} \] of peppers are yellow, of which 80\% are organic.

A pepper is chosen at random.

\[\frac{5}{20} \] of peppers are yellow, of which 80\% are organic.

\[\frac{5}{20} \] of peppers are yellow, of which 80\% are organic.

\[\frac{5}{20} \] of peppers are yellow, of which 80\% are organic.

\[\frac{5}{20} \] of peppers are yellow, of which 80\% are organic.

\[\frac{5}{20} \] of peppers are yellow, of which 80\% are organic.

| Exercise 8 | Calc.: X |
|---|-------------------|
| In a football team composed of 18 players, 3 are goalkeepers, 5 are defenders, 6 are mi | idfielders |
| and 4 are forwards. | |
| a) The trainer chooses 3 of those defenders to play the next match. | |
| Calculate how many different groups of three defenders the trainer can choose. | 1 mark |
| b) The three defenders have been chosen. Now, one of them is assigned the left part of one of them is assigned the central part, and one of them is assigned the right part | , i |
| Calculate in how many different ways those 3 defenders can position themselves on | the field. 1 mark |
| c) 11 players are to be selected to play the game: this team will consist of 1 goalkeep fenders, 5 midfielders and 2 forwards. | er, 3 de- |
| The 3 defenders have been chosen. | |
| Determine how many different groups of 8 players the trainer can choose to fill the replaces. | emaining 3 marks |

A brewery has a machine that fills bottles with soft drinks. The machine is set up so that the quantity of soft drink filled in a bottle is normally distributed with a mean of 505 ml and a standard deviation of 2 ml.

a) **Determine** the probability that a randomly chosen bottle contains at least 505 ml of soft drink.

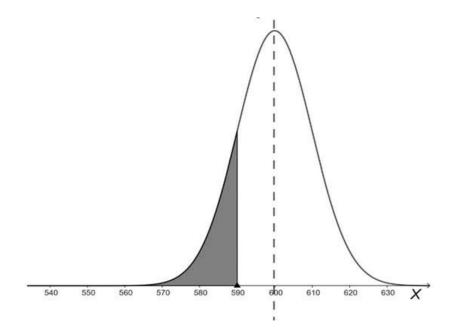
1 mark

b) **Determine** the probability that a randomly chosen bottle contains between 501 ml and 509 ml of soft drink.

 $1 \, \text{mark}$

c) Another machine fills bottles with juice. It is assumed that the quantity of juice contained in a bottle follows a normal distribution with mean μ ml and standard deviation σ ml. It is given that $P(X \le 590) = 0,1587$.

The graph of this normal distribution is given below.



Give the value of the mean of this normal distribution and justify your answer.

1 mark

d) **Determine** the probability that a randomly chosen bottle contains more than 590 ml of juice. **Give** the answer to the nearest tenth.

2 marks

Exercise 10 Calc.: X

In a population of fish, approximatively 42% are female. A test is conducted because it is possible that, in fact, this proportion is less.

a) State the null hypothesis H_0 and the alternative hypothesis H_1 .

2 marks

b) Let X be the random variable that gives the number of female fish in a sample of 20 fish. The table below shows values of $P(X \le k)$ for k = 3, 4, 5, 6, 7, 8, for a probability of 42% that a given fish is a female.

| k | 3 | 4 | 5 | 6 | 7 | 8 |
|--------------|--------|--------|--------|--------|--------|--------|
| $P(X \ge k)$ | 0.0102 | 0.0349 | 0.0922 | 0.1959 | 0.3461 | 0.5229 |

Determine the critical value k if the significance level is set at 5%, and **interpret** this value.

3 marks