The Belgian "Loterie Nationale" organizes many games, one of them is the Lotto. In this game, there are 45 different numbers on 45 different balls, and 6 balls are chosen, randomly. When you play this game, you choose 6 numbers, and you win if you have chosen the 6 numbers that are on the 6 random balls. See https://en.wikipedia.org/wiki/Six-number_lottery_game.

Encore 2j 4h 30min											Ce mercredi 28 avril € 1.000.000 [*] à gagner [*] Si vous êtes le seul gagnant au rang 1																							
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11 16 21 26	7 12 17 22 27 32	8 13 18 23 28 33	9 14 19 24 29 34	10 15 20 25 30	11 16 21 26 31	7 12 17 22 27 32	8 13 18 23 28	9 14 19 24 29 34	10 15 20 25 30 35	11 16 21 26 31	7 12 17 22 27	8 13 18 23 28 33	9 14 19 24 29 34	10 15 20 25 30 35	11 16 21 26 31	7 12 17 22 27 32	8 13 18 23 28	9 14 19 24 29 34	10 15 20 25 30 35	6 11 16 21 26 31	7 12 17 22 27 32	8 2 13 7 18 2 23 7 28	9 14 19 24 29 34	10 15 20 25 30	6 11 16 21 26	7 12 17 22 27 32	8 13 18 23 28 33	9 14 19 24 29 34	10 15 20 25 30 35	6 11 16 21 26 31	7 12 17 22 27 32	8 13 18 23 28 33	9 3 14 3 19 3 24 3 29	10 15 20 25 30 35
11 16 21 26 31 36	7 12 17 22 27 32 37	8 13 18 23 28 33 38	9 14 19 24 29 34 39	10 15 20 25 30 35	11 16 21 26 31 36	7 12 17 22 27 32 37	8 13 18 23 28 33	9 14 19 24 29 34 39	10 15 20 25 30 35 40	11 16 21 26 31 36	7 12 17 22 27 32	8 13 18 23 28 33 38	9 14 19 24 29 34 39	10 15 20 25 30 35 40	11 16 21 26 31 36	7 12 17 22 27 32 37	8 13 18 23 28 33	9 14 19 24 29 34 39	10 15 20 25 30 35 40	6 11 16 21 26 31 36	7 12 17 22 27 32 37	8 2 13 7 18 2 23 7 28 2 33 7 38	9 14 19 24 29 34	10 15 20 25 30 35 40	6 11 16 21 26 31 36	7 12 17 22 27 32	8 13 18 23 28 33 38	9 14 19 24 29 34 39	10 15 20 25 30 35 40	6 11 16 21 26 31 36	7 12 17 22 27 32 37	8 13 18 23 28 33 38	9 3 14 3 19 3 24 3 29 3 34	10 15 20 25 30 35 40

Source: https://www.e-lotto.be/FR/drawGames/lotto/play/single/board

The objective of this project is to program different ways to play this game.

1 Without Python

First, we consider the function "naive_random_integers", in Figure 1.

```
Variables:

i is an integer.

chosenIntegers is an array of integers.

Instructions of the function:

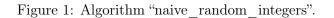
1 chosenIntegers \leftarrow 6 * [0] (An array of size 6 filled with 0)

2 For i from 0 to 5

3 chosenIntegers[i] \leftarrow randint(1, 45) (A random integer between 1 and 45)

4 End For

5 Return chosenIntegers
```



1. Explain what does the algorithm "naive_random_integers". What constraint of the real Lotto is missing here? What should this algorithm do to overcome this limitation? (it is not asked to modify the algorithm)

To overcome the limitation of our first algorithm, we will use an auxiliary array to remember which numbers were already chosen by the algorithm, to avoid choosing them once more. We now consider the function "random_booleans", in Figure 2. In this algorithm, nbIntegers represents the number of integers chosen; result represents a random integer; hasBeenChosen is an array of 45 booleans: it is initially filled with False, and a cell is changed to True when the number corresponding to the index of the cell is chosen by the algorithm).

Variables: *nbIntegers* and *result* are integers. hasBeenChosen is an array of booleans. Instructions of the function: $hasBeenChosen \leftarrow 45 * [False]$ (An array of size 45 filled with False) 1 2 $nbIntegers \leftarrow 0$ $\mathbf{3}$ While nbIntegers < 6 $result \leftarrow randint(1, 45)$ 4 5If not(hasBeenChosen[result - 1]), Then 6 $hasBeenChosen[result - 1] \leftarrow True$ 7 $nbIntegers \leftarrow nbIntegers + 1$ 8 Enf If 9 End While 10Return hasBeenChosen

Figure 2: Function "random_booleans".

- 2. What is the purpose of the condition "If not(hasBeenChosen[result 1])" on line 5?
- 3. Please complete the function "random_integers" in Figure 3. This function uses the function "random_booleans" given in the previous question.

Variables: *idBool* and *idInt* are integers. randomBooleans is an array of booleans. randomIntegers is an array of integers. Instructions of the function: $randomBooleans \leftarrow random \ booleans()$ (A call to the previous algorithm) 1 $\mathbf{2}$ $randomIntegers \leftarrow [0, 0, 0, 0, 0, 0]$ 3 $idInt \leftarrow 0$ 4 For idBool from 0 to 44, Do $\mathbf{5}$ 6 $randomIntegers[idInt] \leftarrow idBool + 1$ 7 $idInt \leftarrow idInt + 1$ 8 Enf If 9 End For 10 Return randomIntegers

Figure 3: Function "random_integers".

2 With Python

- 4. Write in Python the functions "random_booleans" and "random_integers".
- 5. Write in Python a new function that asks the user 6 numbers (the ones they wish to play), runs the function "random_integers" to get another array of 6 random numbers, compare the two arrays, and displays the numbers that are in both arrays.

BONUS Output an error when the user gives twice the same number in their input.