In this sequences of works, we will for the first time create new object types (classes). We will create the Tree class, which we'll use to manipulate trees, see Listing 1.

```
class Tree:
    def __init__(self, data, left=None, right=None):
        self.data = data
        self.left = left
        self.right = right

def __str__(self):
    return str(self.data)
```

Listing 1: The Tree data structure.

In this data structure, each tree can either be an empty tree (None), or contains some data, and has two children (the left and right children). Listing 2 is an example of use with mathematical expressions. You can download it from http://www.barsamian.am/2021-2022/S7ICTA/TP9_Trees.py.

```
two = Tree(2)
   four = Tree(4)
   five = Tree(5)
3
   thirteen = Tree(13)
4
   tree1 = Tree("^", two, five)
   tree2 = Tree("*", four, thirteen)
   alsacian_tree = Tree("*", tree1, tree2)
7
9
   def print_tree(tree):
10
       if tree is None: return
11
       print_tree(tree.left)
       print(tree.data, end=" ")
12
13
       print_tree(tree.right)
14
   print_tree(alsacian_tree)
15
```

Listing 2: Mathematical expression.

- 1. Draw the tree associated to the variable alsacian_tree.
- 2. What is the result of the mathematical expression in alsacian_tree?
- 3. Define a new tree final_tree associated to the expression $(13+8) \times 2$.
- 4. What is printed if you call the function print_tree on this tree? Can you modify this function so that the printing gives the correct mathematical value when read?
- 5. Write a function compute_tree that computes the mathematical result of an expression contained in a tree. You can assume that the field data only contains numbers, or the strings +, -, *, / and ^.
- BONUS All trees seen in this work are either None, or a number, or an operator (that requires two sub-expressions). How would you handle other mathematical expressions like $\sqrt{5}$, i.e. expression that use functions with only one sub-expression?