# S6 MATHEMATICS - 3 Periods PART B 

DATE: 19 ${ }^{\text {th }}$, December 2018

DURATION OF THE EXAMINATION: 90 minutes

Total: 65 points

With Calculator


NUMBER OF PUPILS: 9

## EXERCISE 1-B:

The figure represents the graph of a derivate function $f^{\prime}$ of a function $f$.

a) Give the $x$-coordinates of the extrema of $f$ and state their nature.
b) From the graph of $f^{\prime}$ find the slope of the tangent to the graph of $f$ at $x=-1$.
c) Find the solutions for $f^{\prime}(x)=6$.
d) The graph of function $f$ passes through point $P(0,1)$. Find the equation of the tangent to the graph of $f$ at point $P$.

## EXERCISE 2-B:

Consider the function $f(x)=-x^{3}-3 x^{2}+5 x+7$ and its graph $F$.
a) Draw a table of signs showing the variations of function $f$.
b) Find the coordinates of the turning points of $F$ and state their nature.

Give answers correct to 1 d.p.
c) Find the equation of the tangent to the graph at $x=-1$.
d) Find the coordinates of the points on $F$ where the tangent has slope 5 .
e) Find the equation of the tangents to $F$ with slope 5 .

## EXERCISE 3-B:

A volleyball player serves from the back line of the court to send the ball into the adversary camp. The height $h$ of the ball, in meters, is given by the following function :
$h(t)=-4.9 t^{2}+3.8 t+1.7$, where $t$ is in seconds.
(For this exercise give all answers correct to 2 d.p.)
a) What is the maximum height reached by the ball?
b) After how long will the ball fall to the ground?
c) For how long does the ball stay above 1.5 m ?
d) The ball will reach the net at $t=0.6 \mathrm{~s}$. The height of the net is 2.34 m . Will the ball pass over the net into the adversary camp? Explain.

## EXERCISE 4-B:

Consider the function $g(x)=\frac{a x-5}{-3 x+1}$ and its graph $G$.
a) What is the domain of function $g$ ?
b) Give the equation of the vertical asymptote to $G$.
c) $y=-2$ is an asymptote to $G$. Determine the value of $a$.
d) What is the range of function $g$ ?
e) Find the coordinates of the intersections points of $G$ with the $x$ and $y$ axis.
f) Find the intersection points between $G$ and the line $y=x+1$.

## EXERCISE 5-B:

A function $f(x)$ has one local minimum at $(1,-5)$. State the coordinates of the local minimum of the following functions:
a) $f(x-5)+7$
b) $f(x+4)+1$
a) The figure represents the graph of a function $g(x)$. Sketch a possible graph for the function $g^{\prime}(x)$ on the same grid.

b) The figure represents the graph of a derivate function $f^{\prime}(x)$. Sketch a possible graph for the function $f(x)$ on the same grid.


