## MATHEMATICS 3 PERIODS <br> PART A

## DATE: DD/MM/YYYY

## DURATION OF THE EXAMINATION: 120 minutes

## EXAMINATION WITHOUT TECHNOLOGICAL TOOL

## AUTHORISED MATERIAL:

## Formula Booklet

## Notes:

- As this is a sample paper the cover page is likely to change.
- This sample paper should only be used to see how questions can be created from the syllabus focusing on competences rather than strictly on content.
- The keywords found in the syllabus are highlighted in bold to help the candidate see which competency the question is focusing on and thus helping in answering the question.



| PART A |  |  |
| :---: | :---: | :---: |
|  | Page 3/4 | Marks |
| S6 | The number of bacteria in a petri dish is investigated in a laboratory. It turns out, that under certain conditions, the growth can be modelled by the function $N(t)=10000 \cdot e^{\ln (1,03) \cdot t}$ <br> where $N(t)$ is the number of bacteria after $t$ days. <br> a) Give the number of bacteria at the beginning and the growth rate in percent. <br> b) Calculate the number of bacteria after the first day. <br> c) Explain, why this model cannot be used on a very large time scale. | 5 |
| S7 | Indicate if the statement is true or false and reason your answer. Note that the points are only given if answer and reason are correct. <br> a) If the temperature $T(x)$ is constantly increasing, then $T^{\prime}(x)>0$. <br> b) All periodic models can be modelled by a sine function. <br> c) There are 9 different possibilities for 3 pupils to stand next to each other. <br> d) When some dice is rolled once, the expected value is 3.5 . <br> e) If 10 people are chosen out of a very large group, the number of females can be modelled by a binomial distribution, although a person cannot be chosen more than once. | 5 |
| 58 | The daylength $L(t)$ in hours on a certain location was recorded over one year. It can be modelled by the function $L(t)=4 \cdot \sin \left(\frac{2 \pi}{365} x\right)+12$ <br> where $t$ is the time in days. <br> Interpret the outcome of $\int_{0}^{365} L(t) d t$ and explain, why the result is equal to $12 \cdot 365=4380$. | 5 |
| S9 | a) Interpret what is meant by expected value of a random variable. <br> b) $X$ is a random variable following a normal distribution with expected value $\mu$ and standard deviation $\sigma$. <br> Give a probability taking into account these two characteristic values $\mu$ and $\sigma$. <br> c) A continuous random variable $Y$ defined over $\mathbb{R}$ is such that $P(a \leq y \leq b)=\int_{a}^{b} f(z) d z$. <br> Explain why $\int_{-\infty}^{+\infty} f(z) d z=1$. | 5 |



