## MATHEMATICS 3 PERIODS PART B

DATE: Monday 30th January 2023

## DURATION OF THE EXAMINATION:

2 hours (120 minutes)

## AUTHORISED MATERIAL:

- Examination with technological tool: Calculator Casio Graph $90+E$, Numworks or TI-83 Premium CE Python in exam mode.
- Pencil for the graphs
- Formula booklet


## SPECIFIC INSTRUCTIONS:



- Answers must show the reasoning behind the results or solutions provided.
- Full marks will not be awarded if a correct answer is not accompanied by supporting evidence or explanations of how the results or the solutions have been achieved.
- When the answer provided is not the correct one, some marks can be awarded if it is evident that an appropriate method and/or a correct approach has been used.

NUMBER OF EXAM DOCUMENTS: 2
EXAM DOCUMENTS:

EXAM PAPER
ANSWER BOOKLET
FORMULA BOOKLET

YES $\mathbb{X}$ NO $\square$
YES $\square$ NO $\mathbb{X}$
YES $\mathbb{\text { ® }}$ NO $\square$

## NUMBER OF PAGES OF THE EXAM PAPER: 6

REMINDER: NO ANSWERS TO BE WRITTEN ON THE EXAM PAPER
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NAME OF PUPIL:


EUROPEAN PRE-BACCALAUREATE 2023: MATHEMATICS 3 PERIODS


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| PART B |  |  |
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| QUESTION B2 | Page 1/2 | Marks |
| In the first part of this exercise, we study the cooking of an egg that has just been taken out from a refrigerator. <br> An egg is soft-boiled when its yolk reaches a temperature of exactly $45^{\circ} \mathrm{C}$. <br> In questions a), b) and c), we consider an egg of mass $f(x)$ (in seconds) needed to have the yolk of this egg re (in ${ }^{\circ} \mathrm{C}$ ) is given by: $f(x)=-16 \cdot 60^{2 / 3} \cdot \ln \left(\frac{100-x}{192}\right)$ | ooking time perature $x$ |  |

a) Determine how long it takes for this egg to be soft-boiled. Round to the nearest second.
b) Determine the temperature of the yolk in this egg after it has boiled for 3 marks 240 seconds. Round to the nearest degree.
c) Draw the graph showing the cooking time $f(x)$ as a function of the temperature $x$ in the yolk for this egg, for temperatures between $4^{\circ} \mathrm{C}$ to $45^{\circ} \mathrm{C}$.

In question d), we consider an egg that is soft-boiled after a cooking time of 275 seconds. The following equality applies to the mass $m$ (in grams) of this egg:

$$
275=-16 \cdot m^{2 / 3} \cdot \ln \left(\frac{55}{192}\right)
$$

d) Determine the mass of this egg. Round to the nearest gram.

| PART B |  |  |
| :---: | :---: | :---: |
|  | QUESTION B2 Page $\mathbf{2 / 2}$ | Marks |
| Every morning in a week (7 days), a man is served exactly one egg. Each morning, the probability that the served egg is soft-boiled is $p=0.65$, independently of other mornings. <br> We study the random variable $X$ defined as the number of soft-boiled eggs this man will be served during those 7 mornings. |  | 2 marks |
|  | Determine the probability that this man was served only one soft-boiled egg during those 7 mornings. | 3 marks |
|  | Determine the probability that this man was served soft-boiled eggs for at least 2 mornings in that week. | 3 marks |
|  | We know that this man was served at least two soft-boiled eggs during this week. Determine the probability that he was served exactly three soft-boiled eggs during this week. | 2 marks |
|  | Determine the expected value and the standard deviation of the variable $X$. Interpret those values in the context. | 3 marks |

