

## BAC

SUBJECT	MATHEMATICS 3p
TEACHER	Reynaud E.
DATE	30/1/2023
DURATION (in hours + in minutes)	2 hours (120 minutes)

## AUTHORISED MATERIAL

Formula booklet	
Numworks calculator	

## INSTRUCTIONS / SPECIAL REMARKS

Number all pages and the total number of pages submitted.

All answers must be supported by explanations.

If graphs are used to find a solution, they must be sketched as part of the answer.

Unless indicated otherwise, full marks will not be awarded if a correct answer is not accompanied by supporting evidence or explanations of how the results or the solutions have been achieved.

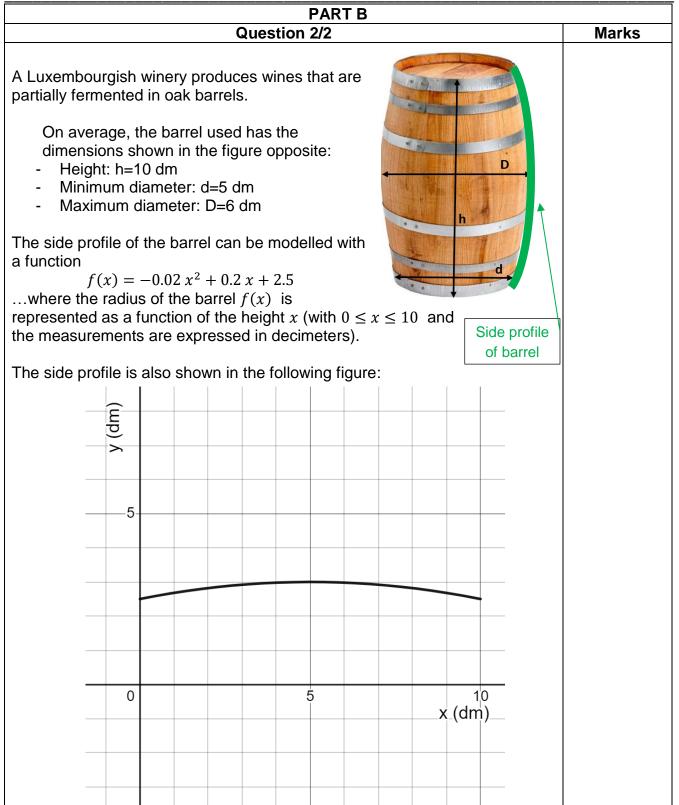


PART B								
Question 1/2	Marks							
The high-speed train (TGV) going to Gare Centrale in Luxembourg City starts slowing down when it passes the train station of the town of Bettembourg. The train velocity, $v$ , in m/s, is given by: v(t) = 84 - 0.3twhere $t$ is the time in seconds after the train has passed the Bettembourg train station.								
For the following questions, you may use the formulae:								
- The distance <i>d</i> (in meters) covered by an object moving at a velocity $v(t)$ between time <i>a</i> and time <i>b</i> is given by: $d = \int_{a}^{b}  v(t)  dt$								
- The acceleration <i>a</i> (in m/s <sup>2</sup> ) of an object moving at a velocity $v(t)$ is given by: $a = \frac{dv(t)}{dt}$ . It can be positive or negative.								
- The thermal energy <i>E</i> (in J, Joules) generated between time <i>a</i> and time <i>b</i> by the TGV train moving at a velocity $v(t)$ is given by: $E = 220000 \int_{a}^{b} v(t) dt$								
a) Find the distance the train has covered in 100 seconds after it has gone through the Bettembourg train station.	2							
<b>b)</b> Calculate the acceleration of the train (here a deceleration).	2							
c) Justify with an appropriate calculation that the train stops 280 seconds after it has gone through the Bettembourg train station, keeping in mind that the train is considered to have stopped when its velocity is equal to zero.	3							
d) During deceleration, there is heat buildup in the brakes of the train due to friction. <b>Calculate</b> the thermal energy generated in the train brakes between the start of the deceleration process in Bettembourg and the point at which the train comes to a complete stop in Gare Centrale.	2							

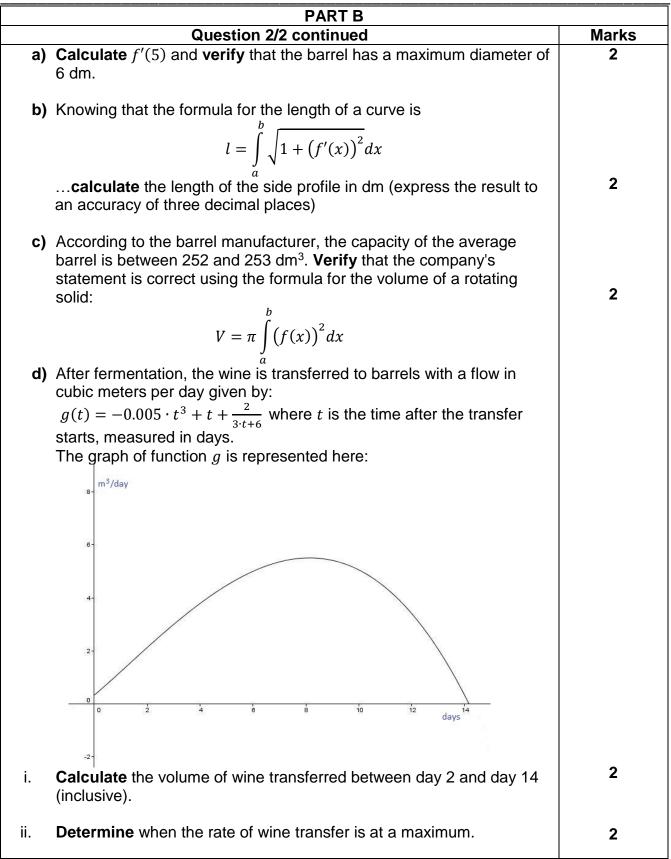


PART B						
	Marks					
The TGV generates noise. The government is investigating using trees and bushes to mitigate the effects of this noise. Through dense foliage, the train noise attenuation <i>A</i> , measured in decibels per meter, dB/m, is given by the following model: $A(x) = -0.058 + 0.0177 \cdot \ln(x)$ where <i>x</i> is the propagation distance of the noise, measured in meters from the train.						
e)	<b>Calculate</b> the attenuation right past the bushes, 30 meters away from the train.	3				
f)	<b>Find</b> the minimal distance away from the train that provides an attenuation of at least 0.04 dB/m.	3				
g)	<b>Discuss</b> the limit of the attenuation value when the propagation distance approaches infinity.	2				
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h)	<b>Determine</b> the probability that none of the persons reach their train with a delay.	2				
i)	Find the probability that at least 200 of the persons reach their train on time.	2				
j)	<b>Find</b> the probability that less than 90% of this group will reach their train on time.	2				
k)	<b>Calculate</b> the expected value and the standard deviation of <i>X</i> .	2				











PART B												
Question 2/2 continued									Marks			
Part of the wine produced is used to make a liquor wine for aging. As the years pass, the wine evaporates. The following table shows the amount of wine left $w(t)$ in a barrel filled in the year 1990, with respect to time $t$ (in years), with $t$ starting from $t$ =1990.												
t (year)	1990	1991	1992	1993	1994	1995	1996	1997	1998	1999	2000	
Wine left (liters)	252	252	251	251	249	247	244	244	243	240	239	
<ul> <li>Enter the data into your calculator.</li> <li>e) Interpreting the trend observed in the data for liquid remaining as a function of year, explain why the data appear to be correlated.</li> </ul>								1				
f) Assuming a linear model can be applied, determine the equation of the linear regression line. Give the coefficients of the equation with a precision of two decimal places.								2				
g) Determine the linear regression coefficient with a precision of two decimal places. Interpret the result; is the correlation reliable?								1				
<b>h)</b> For this question, we will take: $w(t) = -1.418t + 3076$ . <b>Estimate</b> how much wine will be left in a barrel after 20 years (your answer should be correct to the nearest liter).								2				
The wine is finally sold in bottles. The promotional campaign for the product requires that the inside of the bottle cap contains a code that gives the buyer a chance to win a prize with a probability $p = 0.093$ . In a shopping center, 100 bottles are simultaneously displayed.												
i) Justify the fact that one can use a binomial distribution with probability $p$ to model this situation.									1			
j) C	Calcula	te the	mean v	alue a	nd varia	ance of	the bir	nomial	distribu	ition.		2
k) Calculate the probability (with a precision of 4 decimal places) that there are at least 2 bottles out of 100 with a winning cap.									2			
				ility (wi of 100 v				cimal p	places)	that th	ere are	2
m) Calculate the probability (with a precision of 4 decimal places) that there are a maximum of 10 bottles out of 100 with a winning cap.									2			



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